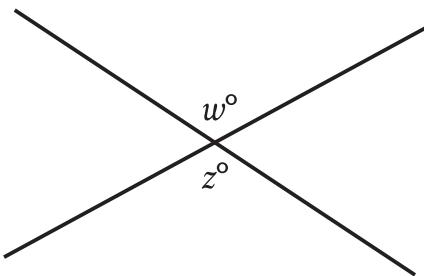


# Question ID 0e245a77

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: 0e245a77



Note: Figure not drawn to scale.

In the figure, two lines intersect at a point. If  $w = 136$ , what is the value of  $z$ ?

- A. 36
- B. 44
- C. 68
- D. 136

ID: 0e245a77 Answer

Correct Answer: D

Rationale

Choice D is correct. In the figure shown, the angles with measures  $w^\circ$  and  $z^\circ$  are vertical angles. Since vertical angles are congruent,  $w = z$ . Therefore, if  $w = 136$ , the value of  $z$  is 136.

Choice A is incorrect and may result from conceptual or calculation errors.

Choice B is incorrect. This is the measure, in degrees, of an angle that's supplementary, not congruent, to the angle with measure  $w^\circ$ .

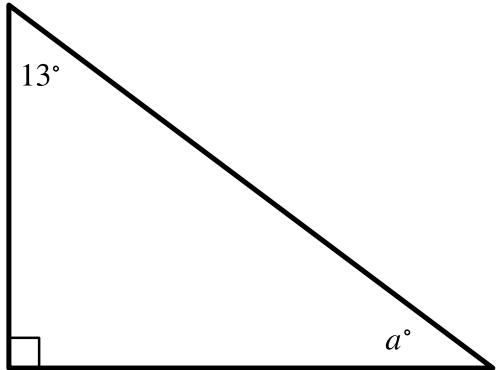
Choice C is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium

# Question ID f9addc5d

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: f9addc5d



Note: Figure not drawn to scale.

In the right triangle shown, what is the value of  $a$ ?

- A. 13
- B. 77
- C. 90
- D. 103

ID: f9addc5d Answer

Correct Answer: B

Rationale

Choice B is correct. The triangle shown is a right triangle, where the interior angle shown with a right angle symbol has a measure of  $90^\circ$ . It's shown that the other two interior angles measure  $13^\circ$  and  $a^\circ$ . The sum of the measures of the interior angles of a triangle is  $180^\circ$ ; therefore,  $90 + 13 + a = 180$ . Combining like terms on the left-hand side of this equation yields  $103 + a = 180$ . Subtracting  $103$  from both sides of this equation yields  $a = 77$ .

Choice A is incorrect. This is the measure, in degrees, of the other acute interior angle of the right triangle, not the value of  $a$ .

Choice C is incorrect. This is the measure, in degrees, of the right angle of the right triangle, not the value of  $a$ .

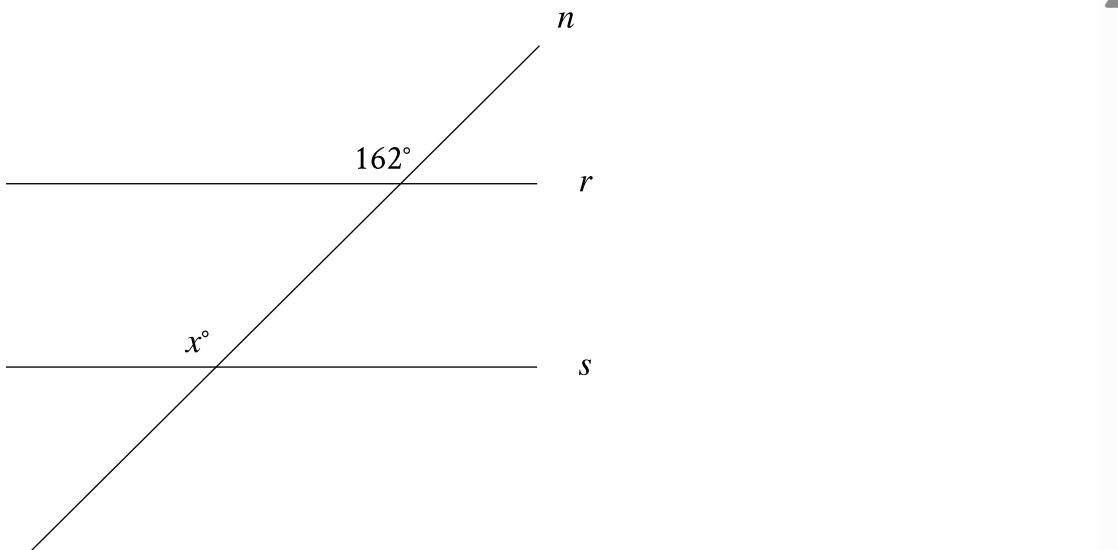
Choice D is incorrect. This is the sum of the measures, in degrees, of the other two interior angles of the right triangle, not the value of  $a$ .

Question Difficulty: Medium

# Question ID 77fea3f6

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: 77fea3f6



Note: Figure not drawn to scale.

In the figure, line  $n$  intersects lines  $r$  and  $s$ . Line  $r$  is parallel to line  $s$ . What is the value of  $x$ ?

ID: 77fea3f6 Answer

Correct Answer: 162

Rationale

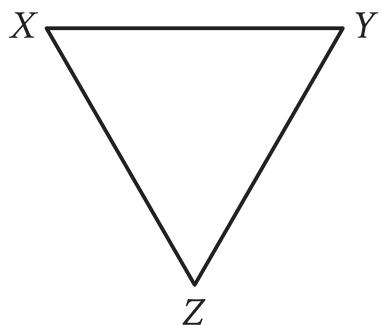
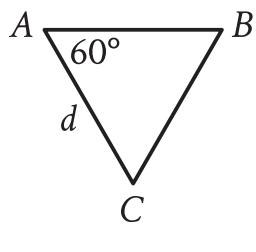
The correct answer is **162**. It's given that line  $r$  is parallel to line  $s$ . Since line  $n$  intersects both lines  $r$  and  $s$ , it's a transversal. The angles in the figure marked as  $162^\circ$  and  $x^\circ$  are on the same side of the transversal, where one is an interior angle with line  $s$  as a side, and the other is an exterior angle with line  $r$  as a side. Thus, the marked angles are corresponding angles. When two parallel lines are intersected by a transversal, corresponding angles are congruent and, therefore, have equal measure. It follows that the value of  $x$  is **162**.

Question Difficulty: Medium

# Question ID 6cb8d47f

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: 6cb8d47f



Note: Figures not drawn to scale.

For the triangles shown, triangle  $ABC$  is dilated by a scale factor of 3 to obtain triangle  $XYZ$ , where  $d = 16$ . What is the measure, in degrees, of angle  $X$ ?

- A. 20
- B. 57
- C. 60
- D. 63

ID: 6cb8d47f Answer

Correct Answer: C

Rationale

Choice C is correct. It's given that triangle  $XYZ$  is obtained by a dilation of triangle  $ABC$ . It follows that triangle  $ABC$  is similar to triangle  $XYZ$ , where  $A$  corresponds to  $X$ . Since corresponding angles in similar triangles have the same measure and the measure of angle  $A$  is  $60$  degrees, it follows that the measure of angle  $X$  is also  $60$  degrees.

Choice A is incorrect and may result from conceptual errors.

Choice B is incorrect and may result from conceptual errors.

Choice D is incorrect and may result from conceptual errors.

Question Difficulty: Medium

# Question ID 61c79894

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: 61c79894

Triangles  $EFG$  and  $JKL$  are congruent, where  $E$ ,  $F$ , and  $G$  correspond to  $J$ ,  $K$ , and  $L$ , respectively. The measure of angle  $E$  is  $45^\circ$  and the measure of angle  $F$  is  $20^\circ$ . What is the measure of angle  $J$ ?

- A.  $20^\circ$
- B.  $45^\circ$
- C.  $135^\circ$
- D.  $160^\circ$

ID: 61c79894 Answer

Correct Answer: B

Rationale

Choice B is correct. It's given that triangles  $EFG$  and  $JKL$  are congruent such that angle  $E$  corresponds to angle  $J$ . Corresponding angles of congruent triangles are congruent, so angle  $E$  and angle  $J$  must be congruent. Therefore, if the measure of angle  $E$  is  $45^\circ$ , then the measure of angle  $J$  is also  $45^\circ$ .

Choice A is incorrect. This is the measure of angle  $K$ , not angle  $J$ .

Choice C is incorrect and may result from conceptual or calculation errors.

Choice D is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium

## Question ID ae474eb4

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

**ID: ae474eb4**

In  $\triangle XYZ$ , the measure of  $\angle X$  is  $23^\circ$  and the measure of  $\angle Y$  is  $66^\circ$ . What is the measure of  $\angle Z$ ?

- A.  $43^\circ$
- B.  $89^\circ$
- C.  $91^\circ$
- D.  $179^\circ$

**ID: ae474eb4 Answer**

Correct Answer: C

Rationale

Choice C is correct. The triangle angle sum theorem states that the sum of the measures of the interior angles of a triangle is  $180^\circ$ . It's given that in  $\triangle XYZ$ , the measure of  $\angle X$  is  $23^\circ$  and the measure of  $\angle Y$  is  $66^\circ$ . It follows that the measure of  $\angle Z$  is  $(180 - 23 - 66)^\circ$ , or  $91^\circ$ .

Choice A is incorrect and may result from conceptual or calculation errors.

Choice B is incorrect. This is the sum of the measures of  $\angle X$  and  $\angle Y$ , not the measure of  $\angle Z$ .

Choice D is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium

# Question ID 020141da

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

**ID: 020141da**

In a right triangle, the measure of one of the acute angles is  $51^\circ$ . What is the measure, in degrees, of the other acute angle?

- A. **6**
- B. **39**
- C. **49**
- D. **51**

**ID: 020141da Answer**

Correct Answer: B

Rationale

Choice B is correct. The sum of the measures of the interior angles of a triangle is  $180$  degrees. Since the triangle is a right triangle, it has one angle that measures  $90$  degrees. Therefore, the sum of the measures, in degrees, of the remaining two angles is  $180 - 90$ , or  $90$ . It's given that the measure of one of the acute angles in the triangle is  $51$  degrees. Therefore, the measure, in degrees, of the other acute angle is  $90 - 51$ , or  $39$ .

Choice A is incorrect and may result from conceptual or calculation errors.

Choice C is incorrect and may result from conceptual or calculation errors.

Choice D is incorrect. This is the measure, in degrees, of the acute angle whose measure is given.

Question Difficulty: Medium

## Question ID 9bc228cb

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

### ID: 9bc228cb

In triangle  $ABC$ , the measure of angle  $B$  is  $52^\circ$  and the measure of angle  $C$  is  $17^\circ$ . What is the measure of angle  $A$ ?

- A.  $21^\circ$
- B.  $35^\circ$
- C.  $69^\circ$
- D.  $111^\circ$

### ID: 9bc228cb Answer

Correct Answer: D

#### Rationale

Choice D is correct. The sum of the angle measures of a triangle is  $180^\circ$ . Adding the measures of angles  $B$  and  $C$  gives  $52 + 17 = 69^\circ$ . Therefore, the measure of angle  $A$  is  $180 - 69 = 111^\circ$ .

Choice A is incorrect and may result from subtracting the sum of the measures of angles  $B$  and  $C$  from  $90^\circ$ , instead of from  $180^\circ$ .

Choice B is incorrect and may result from subtracting the measure of angle  $C$  from the measure of angle  $B$ .

Choice C is incorrect and may result from adding the measures of angles  $B$  and  $C$  but not subtracting the result from  $180^\circ$ .

Question Difficulty: Medium

## Question ID 889921f9

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

**ID: 889921f9**

In  $\triangle RST$ , the measure of  $\angle R$  is  $63^\circ$ . Which of the following could be the measure, in degrees, of  $\angle S$ ?

- A. 116
- B. 118
- C. 126
- D. 180

**ID: 889921f9 Answer**

Correct Answer: A

Rationale

Choice A is correct. The sum of the measures of the angles of a triangle is  $180^\circ$ . Therefore, the sum of the measures of  $\angle R$ ,  $\angle S$ , and  $\angle T$  is  $180^\circ$ . It's given that the measure of  $\angle R$  is  $63^\circ$ . It follows that the sum of the measures of  $\angle S$  and  $\angle T$  is  $(180 - 63)^\circ$ , or  $117^\circ$ . Therefore, the measure of  $\angle S$ , in degrees, must be less than  $117$ . Of the given choices, only 116 is less than 117. Thus, the measure, in degrees, of  $\angle S$  could be 116.

Choice B is incorrect. If the measure of  $\angle S$  is  $118^\circ$ , then the sum of the measures of the angles of the triangle is greater than, not equal to,  $180^\circ$ .

Choice C is incorrect. If the measure of  $\angle S$  is  $126^\circ$ , then the sum of the measures of the angles of the triangle is greater than, not equal to,  $180^\circ$ .

Choice D is incorrect. This is the sum of the measures of the angles of a triangle, in degrees.

Question Difficulty: Medium

# Question ID 74343bea

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

**ID: 74343bea**

In  $\triangle XYZ$ , the measure of  $\angle X$  is  $24^\circ$  and the measure of  $\angle Y$  is  $98^\circ$ . What is the measure of  $\angle Z$ ?

- A.  $58^\circ$
- B.  $74^\circ$
- C.  $122^\circ$
- D.  $212^\circ$

**ID: 74343bea Answer**

Correct Answer: A

Rationale

Choice A is correct. The triangle angle sum theorem states that the sum of the measures of the interior angles of a triangle is  $180^\circ$ . It's given that in  $\triangle XYZ$ , the measure of  $\angle X$  is  $24^\circ$  and the measure of  $\angle Y$  is  $98^\circ$ . It follows that the measure of  $\angle Z$  is  $(180 - 24 - 98)^\circ$ , or  $58^\circ$ .

Choice B is incorrect and may result from conceptual or calculation errors.

Choice C is incorrect. This is the sum of the measures of  $\angle X$  and  $\angle Y$ , not the measure of  $\angle Z$ .

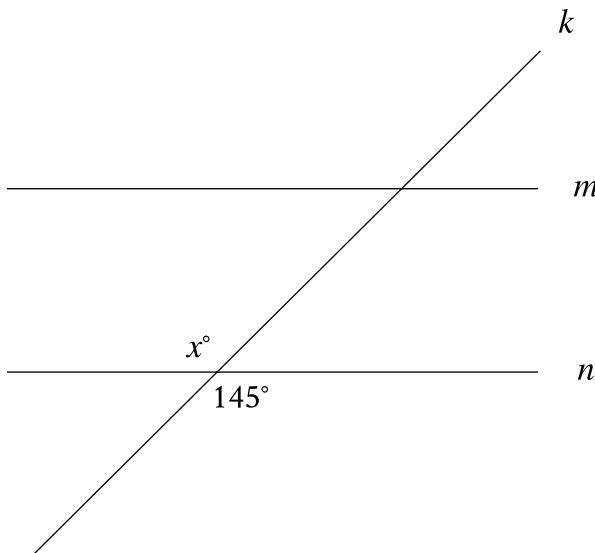
Choice D is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium

# Question ID 832e0f0d

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: 832e0f0d



Note: Figure not drawn to scale.

In the figure, line  $m$  is parallel to line  $n$ , and line  $k$  intersects both lines. Which of the following statements is true?

- A. The value of  $x$  is less than 145.
- B. The value of  $x$  is greater than 145.
- C. The value of  $x$  is equal to 145.
- D. The value of  $x$  cannot be determined.

ID: 832e0f0d Answer

Correct Answer: C

Rationale

Choice C is correct. Vertical angles, or angles that are opposite each other when two lines intersect, are congruent. It's given that line  $k$  intersects line  $n$ . Based on the figure, the angle with measure  $x^\circ$  and the angle with measure  $145^\circ$  are vertical angles. Therefore, the value of  $x$  is equal to 145.

Choice A is incorrect and may result from conceptual or calculation errors.

Choice B is incorrect and may result from conceptual or calculation errors.

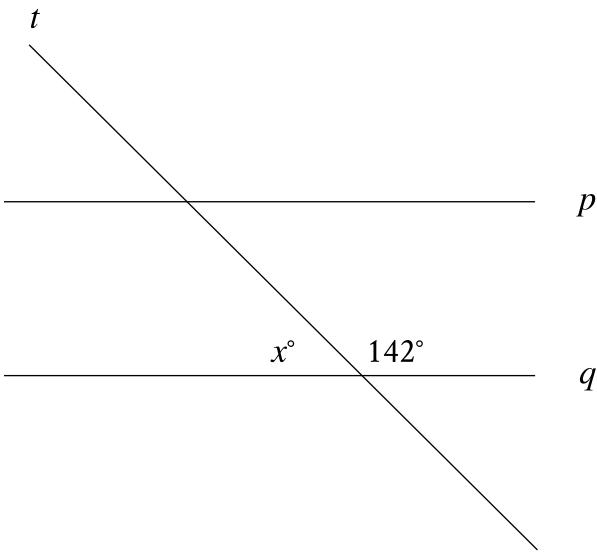
Choice D is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium

# Question ID c0826656

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: c0826656



Note: Figure not drawn to scale.

In the figure, line  $p$  is parallel to line  $q$ , and line  $t$  intersects both lines. What is the value of  $x + 142$ ?

- A. 52
- B. 90
- C. 142
- D. 180

ID: c0826656 Answer

Correct Answer: D

Rationale

Choice D is correct. In the figure shown, the angle marked  $x^\circ$  and the angle marked  $142^\circ$  form a linear pair of angles. If two angles form a linear pair of angles, the sum of the measures of the angles is  $180^\circ$ . Therefore, the value of  $x + 142$  is  $180$ .

Choice A is incorrect. This is  $90$  less than  $142$ , not the sum of  $x$  and  $142$ .

Choice B is incorrect and may result from conceptual or calculation errors.

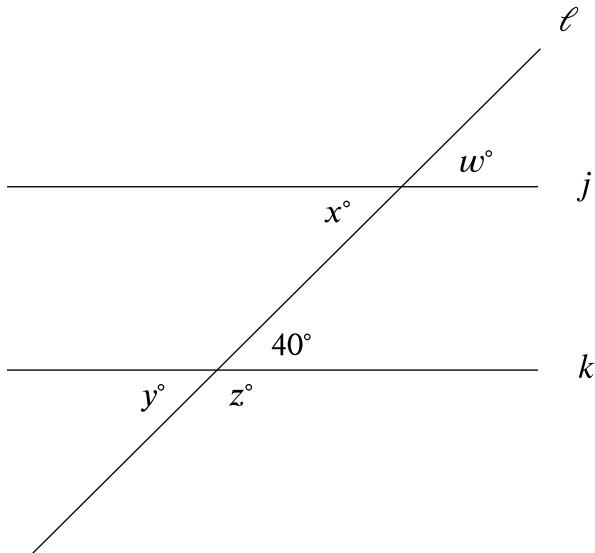
Choice C is incorrect. This is the measure, in degrees, of one of the angles shown.

Question Difficulty: Medium

# Question ID c2518db3

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

ID: c2518db3



Note: Figure not drawn to scale.

In the figure shown, line  $\ell$  intersects lines  $j$  and  $k$ . Which additional piece of information is sufficient to prove that lines  $j$  and  $k$  are parallel?

- A.  $w = 40$
- B.  $x = 140$
- C.  $y = 40$
- D.  $z = 140$

ID: c2518db3 Answer

Correct Answer: A

Rationale

Choice A is correct. In the figure shown, lines  $j$  and  $k$  are parallel if and only if a pair of corresponding angles are congruent. It's given that one angle has a measure of  $40^\circ$  and that the corresponding angle has a measure of  $w^\circ$ . Therefore,  $w = 40$  is sufficient to prove that lines  $j$  and  $k$  are parallel.

Choice B is incorrect. The angle measuring  $x^\circ$  and the angle measuring  $40^\circ$  are alternate interior angles. Thus, if lines  $j$  and  $k$  are parallel,  $x$  is equal to  $40$ , not  $140$ .

Choice C is incorrect. The angle measuring  $y^\circ$  and the angle measuring  $40^\circ$  are vertical angles. Thus,  $y = 40$ , whether lines  $j$  and  $k$  are parallel or not.

Choice D is incorrect. The angle measuring  $z^\circ$  is supplementary to the angle measuring  $40^\circ$ . Thus,  $z = 180 - 40$ , or  $z = 140$ , whether lines  $j$  and  $k$  are parallel or not.

Question Difficulty: Medium

# Question ID 201ae66a

Assessment	Test	Domain	Skill	Difficulty
PSAT 8/9	Math	Geometry and Trigonometry	Lines, angles, and triangles	Medium

**ID: 201ae66a**

In triangle  $ABC$ ,  $AB = 4,680$  millimeters (mm) and  $BC = 4,680$  mm. Which statement is sufficient to prove that triangle  $ABC$  is equilateral?

- A.  $AC = 4,680$  mm
- B.  $AC = 468$  mm
- C.  $AC = 46.8$  mm
- D.  $AC = 4.68$  mm

**ID: 201ae66a Answer**

Correct Answer: A

Rationale

Choice A is correct. In an equilateral triangle, all three sides have the same length. It's given that in triangle  $ABC$ ,  $AB = 4,680$  mm and  $BC = 4,680$  mm. Therefore, if  $AC = 4,680$  mm, then all three sides of triangle  $ABC$  have the same length, so triangle  $ABC$  is equilateral. Therefore,  $AC = 4,680$  mm is sufficient to prove that triangle  $ABC$  is equilateral.

Choice B is incorrect and may result from conceptual or calculation errors.

Choice C is incorrect and may result from conceptual or calculation errors.

Choice D is incorrect and may result from conceptual or calculation errors.

Question Difficulty: Medium